On-board Aging Estimation using Half-cell Voltage Curves for LiFePO$_4$ Cathode-based Lithium-Ion Battery for Electric Vehicle Application

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Abstract

The aim of this work is the design of an algorithm for on-board determination of the actual capacity of a LiFePO$_4$ cathode-based lithium-ion battery in electric vehicle applications. The presented approach is based on the detection of the predominant aging mechanisms (in terms of loss of lithium and loss of active material in both electrodes) through the determination of the single electrode voltage curves. The information related to the characteristic length and position of the voltage plateaus which can be gathered during the battery operation can be used to obtain the actual aging state of the cells. The length of the plateaus depends on the respective position that the voltage curves of the single electrodes have in relation to each other. Relating the change of the plateau characteristics with the possible aging mechanism allows the determination of the actual battery aging state in terms of total cell capacity. The work presents a possible implementation of an algorithm for capacity determination based on the described methodology. The algorithm is validated with various differently aged LiFePO$_4$ cells. Furthermore, the work discusses the ability of the method to detect the actual battery capacity when only part of the quasi-OCV curve is measured. Achieved accuracy and existing limitations are described and discussed in detail.

Keywords: LiFePO$_4$ cells, on-board capacity estimation, aging mechanisms, single electrode voltage curves.

1 Introduction

The online estimation of the actual battery capacity in applications such as electric vehicles (EV) and plug-in hybrid electric (PHEV) is one of the most challenging tasks. The Battery Management System (BMS) has to be able to calculate the total battery capacity during the normal operation, i.e. without the possibility of discharging completely the cell starting from a fully charged state. Further influence of actual temperature and operating current must be considered. As already described in [1][2][3], the total battery capacity can be obtained tracking the partial Ah-Throughput between two defined state-of-charge (SoC) values, as shown in equation (1). These two values have to be detected independently from the actual capacity, e.g. through the relation “open circuit voltage (OCV) – SoC”.

This way of proceeding takes into account that: i) the cell is characterized by a univocal relation OCV-SoC, and ii) this relation does not change dramatically with the battery lifetime. Obviously these conditions are not fully satisfied considering lithium iron phosphate (LFP) cathode based lithium-ion cells. As it is shown in Figure 1, the characteristic flatness of the OCV and the dramatic impact of the aging on its characteristic make the use of equation (1) not possible. Additionally the presence of an evident hysteresis of the OCV make the problem more complicated and challenged.

\[
C_{\text{actual}} = \frac{100}{\frac{\text{SoC}(t_f) - \text{SoC}(t_i)}{\int_{t_i}^{t_f} I \cdot dt}}
\]  

(1)

Figure 1: Comparison between the OCV of a fresh and aged 8 Ah high power LFP/C cell.

Therefore, new methodologies for the estimation of the cell total capacity of LFP batteries are needed. In the recent years, several researches have focused on the observation of the quasi-OCV of LFP cells during the lifetime [4][5][6]. The change of the characteristics voltage plateaus in terms of length and position during charge and discharge gives direct information of the aging mechanisms which have taken place during the cell lifetime. Therefore a direct link between those characteristics and the total battery capacity exists. Once the total quasi-OCV curve is known, the offline analysis of the single plateaus can be carried out through an incremental capacity analysis (ICA) [7] or an incremental voltage analysis (DVA) [8]. Both methodologies are based on the differentiation of the measured voltage curves. This operation can be hardly carried out online with satisfactory results, due to the highly noisy voltage signal, which cannot deliver reliable information unless a correct filtering approach is employed. To overcome this problem Weng et al. [9] develop a new OCV, which parameters can be directly related to the ICA analysis, without the need to carry any differentiation process. For the same reason, Feng et al. [10] introduce the use of the probability density function. The presented methodology is purely mathematic, and therefore it is valid only in a limited number of cases, as only a valid mathematical solution of the problem is found. Interesting and promising approaches are introduced in [5][6][11]. The authors, through simple equation, have related the total capacity of the anode and cathode electrode with the single battery aging mechanisms. Once these degradation modes are known, the single voltage electrode curves can be obtained, and therefore the total voltage curve can be calculated. Finally the total capacity and the actual stoichiometry of the cell can be estimated.

Following these research lines, we propose a novel methodology based on the detection of the single aging mechanism which can be employed online to obtain the total capacity of the battery in LFP cells. Once the characteristic of the voltage plateaus in terms of length and position are tracked online, the aging mechanisms can be modified in order to find the correct position (stoichiometry) and dimension (total electrode capacity) of the single voltage electrode curve of a fresh cell. The obtained results allow the calculation of the actual battery capacity. The work is structured as follows. Chapter 2 introduces a novel structure concept of a BMS for LFP cells for capacity estimation, where also the recalibration of possible hysteresis model is shown. Chapter 3 describes the core of the aging detection algorithm for total capacity estimation. Chapter 4 presents the results and discusses the possible merits and drawbacks of the presented methodology. Chapter 5 closes the work with the conclusion.

2 Novel concept of BMS aging detection subsystem for LiFePO₄ cells

The particular characteristics of LFP cells (e.g. flatness of the OCV curve and hysteresis behaviour) entail the necessity to develop a new concept of BMS, which differs from the one generally used for traditional lithium-ion batteries [12]. In Figure 2, a novel concept of aging detection subsystems of BMS for LFP cells is introduced. The estimation of the state-of-health (SoH) of the battery, especially in term of total actual capacity, takes place in 2 steps.
The first step is the online observation of the cell voltage behaviour to gather the information regarding the position and length of the voltage plateaus. This can be achieved in two ways. The first method consists of the observation of the battery voltage during the charging process. It is required that the charging process takes place under constant current condition, with a current rate limited (current smaller than 0.3C are sufficient) so that the plateau can be clearly detected. These two conditions can be easily satisfied in an EV or PHEV. The second method consists of the observation of the battery voltage under load, e.g. under driving conditions. By means of an equivalent battery circuit model [13][14], once the passive parameters have been properly adapted, the OCV of the battery can be calculated backwards. The advantage is that the value of the obtained OCV must not be precise in terms of value, but only in the length and position of the single plateaus. Furthermore, for both methodologies, on the one hand it is not needed that all the existing plateaus are measured consecutively; on the other hand, it is necessary to measure the single plateaus completely, since the partial measure does not give any information regarding total length and position. The gathered plateau information is then pre-processed and scaled to the reference conditions considering the actual ambient temperature and the current rate. Then the information is saved and ready to be processed.

The second step is the offline processing of the gathered information for SoH estimation. With the term “offline” the possibility to process the information in period of time where the BMS microcontroller is under limited load is meant (e.g. during night or during rest periods). Through the variation of the values of the aging mechanisms, (the meaning will be clarified in the next section) the two anode and cathode voltage curves are varied in dimension and position. This is done until the simulated full battery curve presents plateaus with the same characteristics of the measured ones. Once this is achieved, the obtained single electrode voltage curves are employed to calculate the actual battery total capacity. Moreover, the two curves can be employed to re-calibrate a possible hysteresis model integrated in the BMS algorithm for SoC estimation.
In the next section, the aging detection core algorithm shown in Figure 2 will be described and presented. The description and implementation methodologies of the other subsystems are out of the goal of this work.

3 Aging detection core algorithm

3.1 Approach background

The aging detection core subsystem represents the main algorithm which is designated to deliver the actual aging state of the cell in terms of total battery capacity. The method proposed in this work is based on the theories presented in [5][15] which are resumed in Figure 3. When a LFP cell is in a fresh state, the voltage curve of the full cell is characterized by three different plateaus, as shown in the small frame of Figure 3a. These 3 plateaus (associated to the graphite) are visible due to the very flat voltage profile of the cathode electrode (FePO₄). In this electrode the intercalation/deintercalation process takes place through a two-phase transition process. During this process the simultaneous existence of two distinct phases with constant lithium concentration produces a constant voltage potential [16] (plateau A in Figure 3a). On the other hand, the voltage profile of the anode is characterized by 3 two-phase transitions (in reality more phase transitions exist but only 3 are clearly visible [17]), which produce the 3 plateaus I, II and III. The subtraction of the cathode and anode voltage curve produces a full voltage profile with the 3 plateaus IA, IIA and IIIA. The length and position of these 3 plateaus in the voltage profiles of the full cell are directly influenced by the aging mechanisms which take place during the battery lifetime. One of the cell degradation modes for lithium-ion batteries reported in the literature is the loss of lithium inventory (LLI) [5].

![Figure 3](image-url)

Figure 3: Qualitative analysis of the effect of the main degradation modes and their influence in the single electrode voltage curve and full cell voltage curve of a LFP cell. a) Fresh cell, b) effect of the loss of lithium inventory, c) effect of the loss of active material in the positive electrode, d) effect of the loss of active material in the negative electrode.
This takes place mainly through the constant formation and growth of the solid electrolyte interface (SEI), which consumes lithium that cannot be anymore used for the mean cell reaction. Another phenomenon which is cause of LLI is the lithium plating. As shown in Figure 3b), the main consequence of the LLI is the shifting of the cathode voltage curve in respect to the anode curve, with the consequent reduction of the cell capacity and the change of the length of the plateau IIIA (the dotted lines represent the status of the voltage curves for the fresh cell). Another known degradation mode is the loss active material (LAM). This can occur in both of electrodes due to the change of electrode composition or the isolation of some of the active particle from the conductive network [5]. On the one hand, the effect of a LAM on the positive electrode (LAM_{P}) is the shrinking of the cathode voltage curve in respect to the anode with the reduction mainly of the length of the plateau IIIA and, in critical cases also of the plateau IIA (Figure 3c). On the other hand, as shown in Figure 3d), the LAM on the negative electrode (LAM_{N}) produces a shrink of the anode voltage curve in respect to the cathode. This influences directly the length of all 3 plateaus, in different ways depending on the amount of LAM. Moreover, other degradation modes related to the variation of the cell internal resistance are neglected in this work and not considered for the capacity calculation.

### 3.2 Working principle

At this point it is clear that if the information about the single plateaus are gathered online, afterwards they can be used to detect the actual position and dimension of the voltage electrode curves, and therefore to know the actual battery capacity. In order to achieve this, two main issues have to be solved: 1) the measurement of the characteristics of the anode and cathode electrode, and 2) the expression of the relationship between the described degradation modes and the capacity of the single electrodes.

One of the possibilities to measure the anode and cathode voltage curves of a lithium-ion cell is to carry out a post-mortem analysis. In this work, a fresh LFP cell was firstly parameterized by measuring the capacity and quasi-OCV curves with different current rates during charge and discharge process. Then, the cell was disassembled in a glove box under argon atmosphere and 16 mm diameter samples of cathode and anode electrode were collected to build coin half-cells (using pure metallic lithium as a reference counter electrode). The voltage characteristics for each of the electrodes and the capacity were measured during charge and discharge process with constant current for different current rates at ambient temperature. The current rate in the coin cell was scaled in respect to the full cell electrode area, in order to obtain the same overvoltage effect. The value of capacity and the trend of the electrode voltage characteristics of the fresh cell are the starting point of the core algorithm for SoH determination.

In order to express the relationship between the degradation modes and the actual electrode capacities, the cathode and anode voltage curves have to be normalized in respect of the same reference system. As normally in lithium-ion batteries the total capacity of the anode is bigger than the capacity of the cathode [5], in this work the capacities of both electrode are normalized in respect of the total cathode capacity obtained for a fresh cell. Thus, with the obtained normalized scale, the voltage curves of the cathode and anode can now be described considering the start and end value of the electrode capacity in the cathode scale, as shown in Figure 4. With this notation, the subscript \( a \) is referred to the anode, while the subscript \( c \) is referred to the cathode.

![Figure 4: Representation of the variables start cathode capacity (C_{cstart}), start anode capacity (C_{astart}), end cathode capacity (C_{cend}) and end anode capacity (C_{aend}).](image)

With this notation, for a fresh cell, the value of capacity equal to 0 corresponds to the starting value of the full cell curve (in the case shown in Figure 4, \( C_{a\text{start}} = 0 \)), while the value of capacity equal to 1 corresponds to the end value of the full cell curve (in the case shown in Figure 4, \( C_{c\text{end}} = 1 \)). Moreover, in this way, it is possible to have starting capacity values smaller than zero and end capacity values bigger than 1.

Therefore, the characteristic values of start and end capacities for the cathode and anode
electrodes can be expressed as a function of the degradation modes, as expressed in [5][6]:

\[ C_{a,\text{start}}, C_{c,\text{start}}, C_{a,\text{end}}, C_{c,\text{end}} = f(LLI, LAM_{Pe}, LAM_{Ne}) \]  

(2)

The value of the anode and cathode capacity in a defined period of the battery lifetime can be expressed as:

\[
\begin{align*}
C_{a,\text{EOL}} &= C_{a,\text{BOL}} (1 - LAM_{Ne}) \\
C_{c,\text{EOL}} &= C_{c,\text{BOL}} (1 - LAM_{Pe})
\end{align*}
\]  

(3)

where the subscript BOL means begin-of-life, while the subscript EOL means end-of-life. The value of the total cell capacity can then be described as:

\[ C_{\text{cell,EOL}} = \min(C_{a,\text{end}}, C_{c,\text{end}}) - \max(C_{a,\text{start}}, C_{c,\text{start}}) \]  

(4)

### 3.3 Algorithm implementation

The implementation of the core algorithm for total capacity determination is described in Figure 5. Once the online subsystem has collected the information in terms of plateaus, then the aging detection core algorithm can start the calculation:

a) Different parameter set \( P_i \) are generated each one containing different values of the degradation modes \( (P_i = [LLI_i, LAM_{Pe,i}, LAM_{Ne,i}]) \).

b) The cathode and anode voltage curves of the fresh cell and their respective capacity values of the electrodes collected after the post-mortem analysis are available for the fitting process.

c) Each of the parameter set \( P_i \) generated at block a) is applied to the available fresh electrode curves. For each \( P_i \) the respective new electrode voltage curve are obtained applying the equation set (2) and (3).

d) For each of the parameter set \( P_i \) the full cell voltage is reconstructed subtracting the anode voltage from the cathode voltage.

e) Each of the new obtained full cell voltage curves is processed in order to identify the length and position of the available plateaus.

f) The plateaus characteristic of the real cell detected from the online subsystem are available for processing.

g) For each \( P_i \) the error is calculated as the sum of the difference between the measured plateaus (online) and the identified ones (identified in block e).

h) If the obtained error is bigger than a defined threshold \( \varepsilon \), then the fitting process start again from the block a) by the generation of new parameter sets.

i) If the obtained error is smaller than a defined threshold \( \varepsilon \), then the full capacity of the battery is calculated according to equation (4).

The methodology applied to generate the new parameter sets at block a) is the varied-parameters approach. This method is already presented by Waag et al. in [13] and it has been slightly modified and adapted for the specific case. Moreover, in the block g) the value of the error is expressed as:

\[ Err = \sum_{n=1}^{3} |LP_{n,\text{measured}} - LP_{n,\text{fitted}}| \]  

(5)
where the $LP$ represents the length of the $n^{th}$ plateau expressed in Ah. It is not necessary to measure all 3 plateaus: the algorithm is able to find a solution and correct the error even if only the information related to 2 or 1 plateaus is available. This allows the possibility to detect the battery capacity also when the cell is not deeply discharged or charged from an empty state. On the contrary, as shown in the next section, too little information results in a worst accuracy and bigger uncertainty of the obtained results.

4 Results

In this section, the results relative to the aging detection core algorithm are shown and discussed. As a proof of concept, the algorithm has been tested considering the plateau information collected during the charge process with a constant current of 0.1C at ambient temperature of 23 °C. Therefore the considered reference capacity for each sample is the one measured at the same conditions, starting from a cell in an empty state. The described algorithm has been validated with three cells in different aging state. The tested batteries are high power LFP/C cells with 8 Ah of nominal capacity. The characteristics of the tested cells are reported in Table 1.

### 4.1 Fitting results

Figure 6 presents the evolution of the tracked degradation modes during the fitting process of the voltage electrode curves and the evolution of the errors for the cell L50C50. In the reported case it is assumed that the information regarding all 3 plateaus are available. The number of iterations is limited to a maximum value of 150. Figure 6a), 6b) and 6c) show respectively the evolution of the degradation modes LLI, LAMPe and LAMNe. The Figure 6d) shows the evolution of the error related to the single plateau. Each error value is calculated as the difference between the measured and the fitted plateau length. Figure 6e) shows the trend of the total error calculated according to equation (5). As it can be observed, starting from some random set values, after ca. 25 iterations the LAMNe reaches already a stable value around 12%, while the LLI degradation mode reaches the value set in this case as a maximum limit. Therefore after around 30 iterations the LLI degradation modes decreases reaching a stable value around 25% after ca. 80 iterations. In the same way, the value of LAMPe is adapted after ca. 30 iterations and reaches a stable value around 2.6% after ca. 60 iterations. Please notice the different scale on the y axis of Figure 6a), 6b) and 6c). As it is shown in Figure 6d) and 6e) the correction of the error takes place rapidly after ca. 25 iterations, which corresponds to the rapidly change of the LAMNe and LLI degradation modes. The slow change of the LAMPe after 60 iterations has only limited effect on the total error. After 25 iterations, the small change of the degradation modes has not significant impact on the single error, although some small improvement is obtained after 60 iterations. After 150 iterations, the errors of the single plateaus reach a maximum value of 0.0868 Ah, which corresponds to a total error of 0.2287 Ah, demonstrating a good agreement with the measured plateau information. Similar results are achieved with all the cells tested. Furthermore, the starting values of the degradation modes can influence the final results and the convergence of the algorithm, depending on the actual aging state of the tested cell. In this direction, the sensibility of the algorithm should be properly tested, to avoid that the algorithm converges to wrong values or divergences.

<table>
<thead>
<tr>
<th>Name</th>
<th>New cell</th>
<th>Z01C10</th>
<th>Z01C80</th>
<th>L50C50</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aging characteristics</td>
<td>Cell in a fresh state</td>
<td>Cycle with constant current of 1C during charge/discharge with a SoC span of 10% between 45% and 55% SoC at ambient temperature of 30 °C</td>
<td>Cycle with constant current of 1C during charge/discharge with a SoC span of 80% between 10% and 90% SoC at ambient temperature of 30 °C</td>
<td>Calendar aging at ambient temperature of 50 °C and at SoC of 50%</td>
</tr>
<tr>
<td>Capacity / Ah</td>
<td>8.27</td>
<td>6.72</td>
<td>7.18</td>
<td>6.61</td>
</tr>
</tbody>
</table>
A significant improvement can be obtained enhancing the fitting strategy, i.e. changing the degradation modes individually based on the value of the actual error or based on the magnitude of the single plateau errors.

4.2 Capacity estimation results

In order to test the correct convergence of the algorithm, 3 different scenarios are considered. In the first scenario, the on-line algorithm shown in Figure 2) has gathered enough information regarding the 3 plateaus, i.e. position and length. In the second scenario, only the information regarding the plateaus IIA and IIIA (Figure 3a) is available. In the third scenario, only the information regarding the plateau IIIA is available. Therefore, the convergence of the algorithm is tested for the 3 scenarios and for the 3 cells introduced in Table 1. The obtained results are reported in Table 2, 3 and 4. The values of the errors are expressed according to the following relation:

$$Err = \frac{C_{real} - C_{calc}}{C_{real}} \cdot 100$$  \hspace{1cm} (6)$$

where $C_{real}$ represents the value of the actual battery capacity in Ah and $C_{calc}$ is the value of the capacity obtained from the fitting process in Ah.

### Table 2: Results of the simulation for the scenarios number 1 (3 plateaus available).

<table>
<thead>
<tr>
<th>Cell</th>
<th>Calculated capacity / Ah</th>
<th>Error / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z01C10</td>
<td>6.90</td>
<td>2.70</td>
</tr>
<tr>
<td>Z01C80</td>
<td>6.97</td>
<td>2.94</td>
</tr>
<tr>
<td>L50C50</td>
<td>6.77</td>
<td>2.28</td>
</tr>
<tr>
<td>Mean error / %</td>
<td>2.646</td>
<td>0.272</td>
</tr>
<tr>
<td>Standard deviation</td>
<td>0.272</td>
<td></td>
</tr>
</tbody>
</table>

### Table 3: Results of the simulation for the scenarios number 2 (2 plateaus available).

<table>
<thead>
<tr>
<th>Cell</th>
<th>Calculated capacity / Ah</th>
<th>Error / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z01C10</td>
<td>6.59</td>
<td>1.99</td>
</tr>
<tr>
<td>Z01C80</td>
<td>7.30</td>
<td>1.60</td>
</tr>
<tr>
<td>L50C50</td>
<td>6.59</td>
<td>0.24</td>
</tr>
<tr>
<td>Mean error / %</td>
<td>1.276</td>
<td>0.752</td>
</tr>
<tr>
<td>Standard deviation</td>
<td>0.752</td>
<td></td>
</tr>
</tbody>
</table>

### Table 4: Results of the simulation for the scenarios number 3 (1 plateau available).

<table>
<thead>
<tr>
<th>Cell</th>
<th>Calculated capacity / Ah</th>
<th>Error / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z01C10</td>
<td>6.68</td>
<td>0.68</td>
</tr>
<tr>
<td>Z01C80</td>
<td>6.76</td>
<td>5.92</td>
</tr>
<tr>
<td>L50C50</td>
<td>6.60</td>
<td>0.087</td>
</tr>
<tr>
<td>Mean error / %</td>
<td>2.229</td>
<td>2.619</td>
</tr>
<tr>
<td>Standard deviation</td>
<td>2.619</td>
<td></td>
</tr>
</tbody>
</table>

Contrary of what it can be expected, as shown in Table 2, the knowledge of the information of all 3 plateaus does not assure the precise calculation of the total battery capacity. The value of the error is maintained stable between 2% and 3%, with a mean value of 2.646% and standard deviation of 0.272. This means that the algorithm is able to converge to a proper value of the capacity in all the cases, although the error is still significantly high. Considering the results of Table 3, the knowledge of 2 plateaus guarantees always the convergence of the algorithm with errors smaller than 2%, reaching in one of the cases values smaller than 1%. The mean error amounts to 1.276% with a standard deviation of 0.752. This assures again the convergence of the algorithm in each of the case studies, with an improvement of the errors, in spite of the limited amount of
information used. In case of scenario 3, where only the information of one plateau is available, the error in the calculation of capacity is small in 2 cases (< 0.7%). However, in the case of the cell Z01C80 the error increases up to 5.92%. This results in a mean error of 2.229% with a standard deviation of 2.619. The calculated values of errors and standard deviations reported in Table 3, 4 are gathered in Figure 7.

Figure 7: Representation of the mean error and of the respective standard deviation for the 3 case studies.

It can be observed that the minimum mean error is obtained for the case where only 2 plateaus are available. In the other cases (i.e. scenario 1 and 3), the mean error increases, reaching the maximum value for scenario 1 (3 plateaus). On the other hand, the error band, which is represented by the value of the standard deviation, is the minimum for the scenario 1, and it increases with decreasing number of analysed plateaus. The explanation of this behaviour can be found observing carefully the results reported in Table 3, 4 and 5. For the scenario 1 (3 plateaus known), the algorithm always converges to a correct solution and finds a proper value of the final capacity. In fact, the calculated capacity remains always stable in all the 3 cases, around a value of 2.6%, demonstrating the stability of the method. However, the algorithm finds difficulties to find a correct solution (i.e. a correct value of the degradation modes) which can reduce the 3 errors at the same time according to equation (5). In fact, the change of the degradation modes can produce in some cases the reduction of the error related to one single plateau, but at the same time the increase of the error related to the other two. In this way the optimization algorithm can enter inside a close loop and converge to a wrong solution. Considering the scenario number 2, the knowledge of the information related to the plateau IIA and IIIA delivers the best compromise between algorithm stability and calculation error. The algorithm converges in the 3 cases to an error value smaller than 2%. For the cell L50C50 an error near to zero is obtained. This can be probably related to the correct starting values of the degradation modes, which brings to a fast and correct convergence. The limited value of the error comparing to scenario 1 confirms the fact that with less plateau information (only 2), and therefore with an easier value of the error function, the algorithm is able to find easily a solution of the problem which represents better the real behaviour of the battery. This means also that knowing 2 plateaus, namely the plateaus IIA and IIIA, enough information is collected for the estimation of the battery capacity. Eventually, the results obtained from the scenario number 3 confirm the conclusion drawn in the other 2 scenarios. The value of the error obtained for the cell Z01C10 and L50C50 is near to zero, indicating the easiness of the algorithm to converge to a solution, which in this case represents correctly the real behaviour of the battery. Nevertheless, the lack of information (only the plateau IIIA is available) does not assure the convergence in every possible case. This is demonstrated in the case of cell L50C50, where the convergence of the algorithm reduces the value of the plateau error, but does not guarantee the correct convergence to a satisfactory solution. Therefore, at the end of the fitting process, the obtained error amounts to ca. 6%.

Summarizing, it can be stated that the knowledge of the information related to the plateau IIA and IIIA is sufficient to guarantee a correct convergence of the algorithm in all the possible cases with a limited error. In case all 3 plateaus are known, the convergence of the algorithm is also assured, combined with an increase of the total error and a bigger computational effort.

As a final discussion, the following points concerning the presented methodology can be highlighted:

- In order to know the total capacity of a LFP cell, discharging completely the battery starting from a fully charge state is not needed. The information related to the actual battery capacity is contained in the length of the plateau and in their position. The knowledge of them is sufficient to characterize the energy capability of the cell.
- Not all 3 plateaus are needed to calculate correctly the battery capacity. The knowledge of 2 plateaus is enough to reach satisfactory results.
• Not all the plateau information has to be saved and collected at the same time. This means, for instance, that the information of the plateau IIA can be collected during charging, while for the plateau IIIA during discharging. Nevertheless it has to be assured that not long time is passed between the collections of the different information.
• The proposed methodology can run offline, and the information does not need to be processed during their acquisition. This allows the possibility to reduce the computational effort of the microcontroller of the BMS, distributing the requested computational power in a long time period.
• Generally, as already discussed by Waag in [12], an error in the calculation of the capacity smaller than 1% can be considered meaningless. In fact, the measurement in a laboratory environment of the battery capacity under standard condition (at defined current rate and constant ambient temperature) can produce in some cell types an error around 0.6% when two or more measurements are repeated in sequence.

5 Conclusion
In this paper a novel methodology for online battery capacity estimation for LFP cells is presented. This new approach is based on the information contained in the characteristic plateaus present in the voltage curves of this type of cells. In particular, the position and the length of these plateaus are used in order to find the correct position and dimension of the two electrode voltage curves measured for a fresh cell. The value of the measured capacity of the anode and cathode electrode can be directly used to calculate the actual total capacity of the battery. The results shown in the frame of this work demonstrates the ability of the presented methodology to converge to a correct value of the total capacity in almost all cases that have been studied. The knowledge of the information related with 3 plateaus assures the convergence of the algorithm, but deliver a high error in the calculation of the battery capacity, while the knowledge of only one plateau does not assure the convergence, due to the lack of information. The information contained in the plateau IIA and IIIA are enough to guarantee the fast convergence of the algorithm with an error which remains for all the cases limited to less than 2%. The future work will focus on 3 main points:
1. The correct detection of the single plateau during the drive phase through a dynamic load observer algorithm.
2. The correct pre-processing of the plateau information gained during the charge process or during the drive phase, in order to consider the correction factors due to the ambient temperature and to the actual current rate.
3. The improvement of the fitting strategy of the plateaus in terms of proper variation of the degradation modes, in order to guarantee a faster and faultless convergence of the methodology.

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References


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